

The Product Rule:

1. (a) The Product Rule states that:

$$\frac{d}{dx} [u(x)v(x)] = \underline{\hspace{2cm}}$$

- (b) Thus, we can apply the Fundamental Theorem of Calculus and obtain

$$u(x)v(x) = \int \quad + \int \quad .$$

- (c) We can now write $du = u'(x) dx$ and $dv = v'(x) dx$. Rearranging the terms, we get the

<p>Integration by Parts Formula:</p>

In order for this to be useful, the integral on the right needs to be easier than the integral on the left. How do we pick u and dv ? Well, to start with, dv should be easy to integrate!

Examples:

2. $\int x e^x dx$
 $u = \quad dv =$
 $du = \quad v =$

3. $\int_1^2 \ln x dx$
 $u = \quad dv =$
 $du = \quad v =$

4. $\int x \ln x dx$

5. $\int_0^{\pi} x \sin x \, dx$

6. $\int_0^1 x\sqrt{x+1} \, dx$ (Compare to worksheet 7-2, Q15. Which method do you prefer?)

7. $\int_1^2 x^2 e^x \, dx$ (Hint: Integrate by parts twice)

8. $\int \arctan x \, dx$ (Hint: Let $u = \arctan x$.)

9. $\int e^x \cos x \, dx$ (Hint: Integrate by parts twice, and carefully observe the equation you obtain.)

10. $\int x(\ln x)^3 \, dx$ (Hint: Integrate by parts times.)

11. $\int x e^{-x^2} \, dx$ (Hint: Don't work too hard!)